



I³N *Innovative
Integrated
Instrumentation
for Nanoscience*



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High Resolution Electronic Measurements in Nano-Bio Science

The interface between solid & liquid: *how to transfer charge through the electrode*

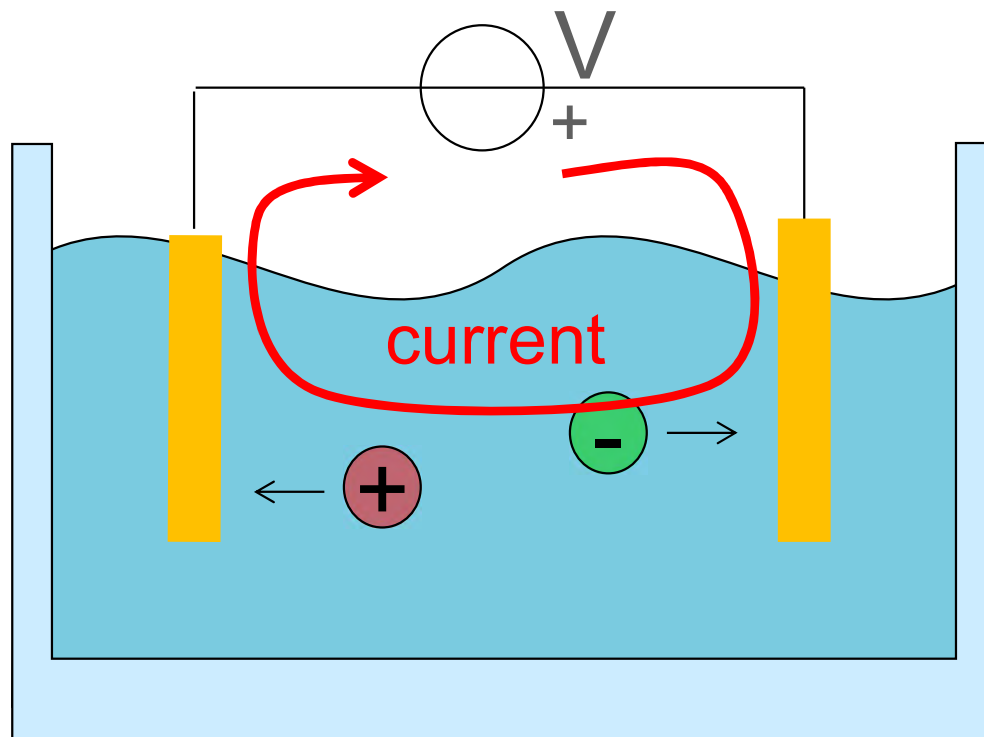
Giorgio Ferrari

Milano, June 2025

Outline

- The electrical behavior of the bulk liquid
- Metal – liquid interface: double-layer capacitance
- Potential drop across the electrode-liquid interface
- Charge transfer at the interface
- Current-Voltage relation

Electrical current in ionic conductors



Ions move in the liquid

Electrons move in the electrodes

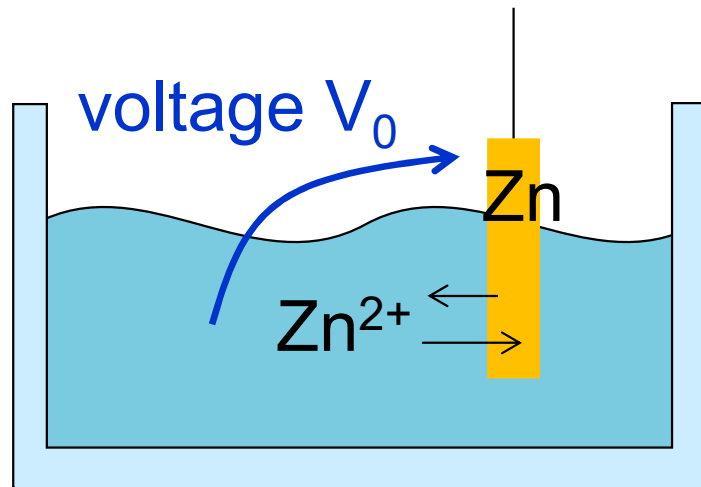
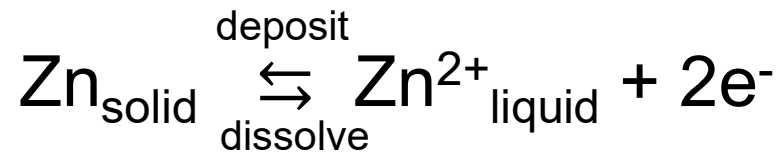


electron transfer at the metal/liquid interface to sustain a DC current

The electron transfer is controlled by the potential difference between the liquid and the electrode:
what are the voltages in our electrochemical cell?

Equilibrium at the interface

Ex.: Zn electrode immersed in a solution with Zn^{2+} ($C_{\text{Zn}^{2+}}$):



Dynamic equilibrium

Zn^{2+} deposit $\rightarrow V_0$ increases $\rightarrow \text{Zn}^{2+}$ repulsed

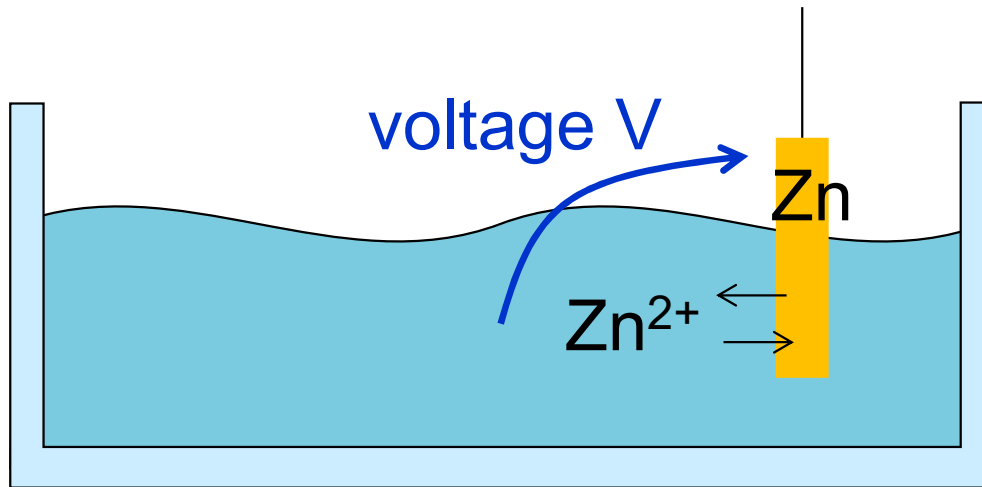
Zn dissolve $\rightarrow V_0$ decreases $\rightarrow \text{Zn}^{2+}$ attracted

The equilibrium condition (no corrosion/deposition, no net charge transfer) is reached with a voltage V_0 determined by:

- metal involved
- ions in solution
- solution
- temperature,...

V_0 is typically not equal to zero.

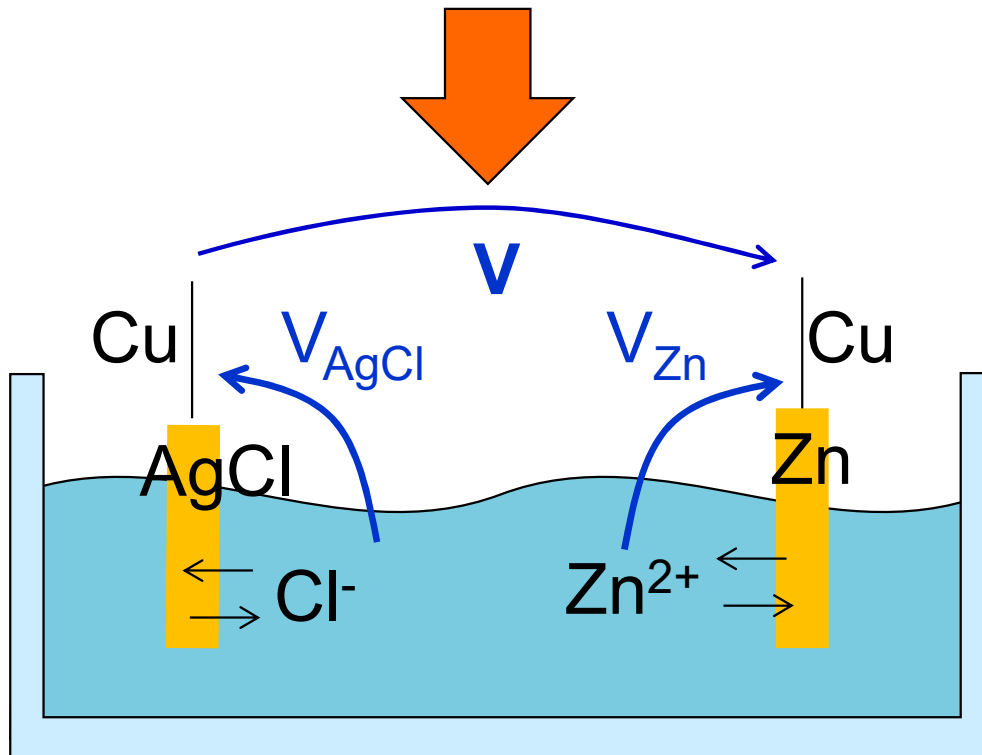
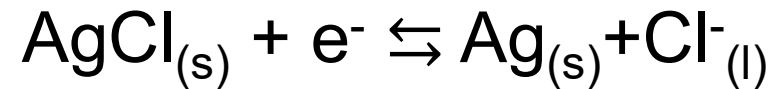
Electrochemical cell



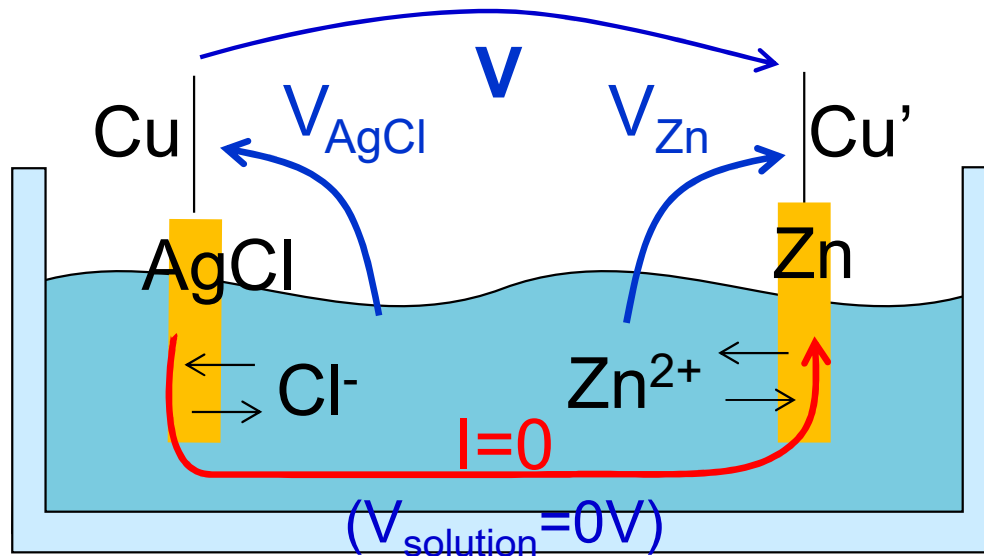
Voltage V is **not** directly measurable using a voltmeter

A 2nd electrode is required!

$$V = V_{\text{Zn}} - V_{\text{AgCl}}$$



Eq. potential of a electrochemical cell



At the equilibrium $I=0$
(no voltage drop in solution)

Depends on Zn, C_{Zn}

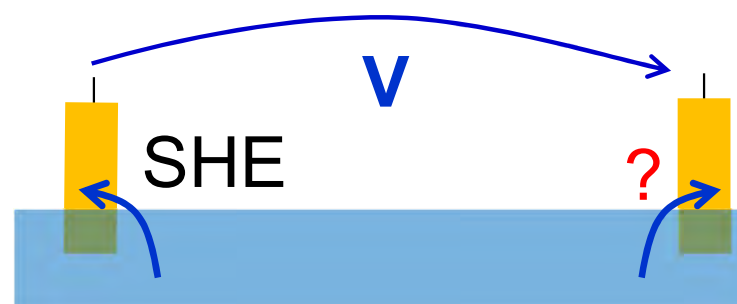
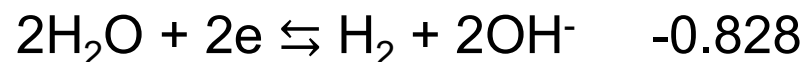
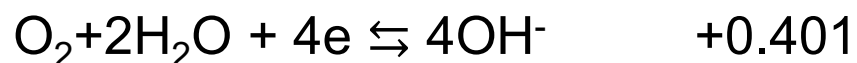
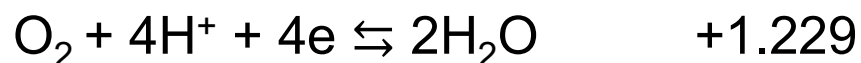
Depends on AgCl, C_{Cl}

$$V = V_{Zn} - V_{AgCl}$$

Equilibrium may require **$V \neq 0V$** (battery!)

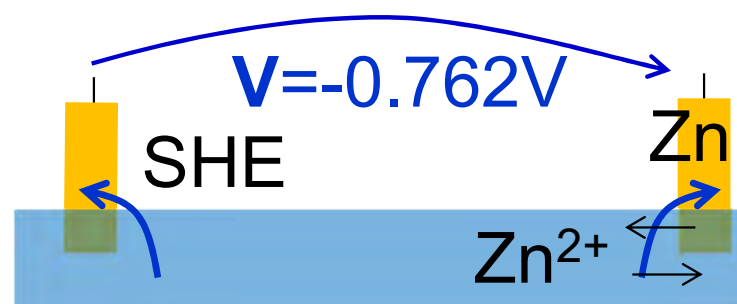
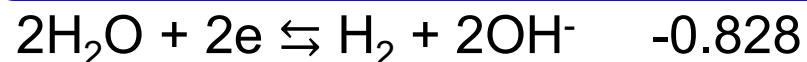
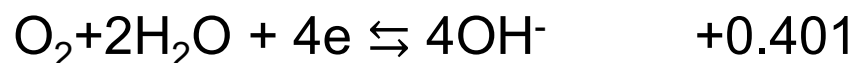
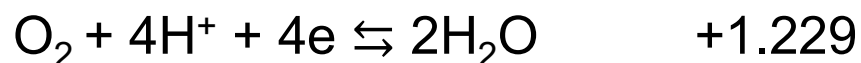
Standard electrode potentials

Aqueous Solutions at 25°C in V vs. SHE (standard hydrogen electrode), 1atm, $C^0=1M$



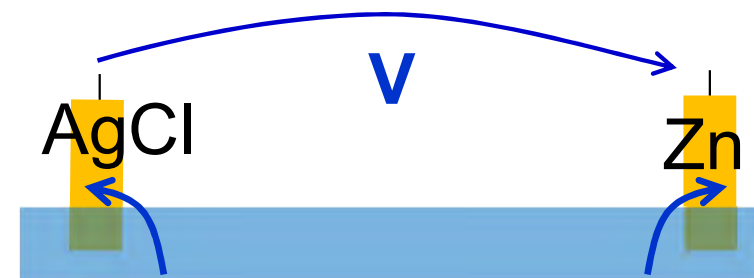
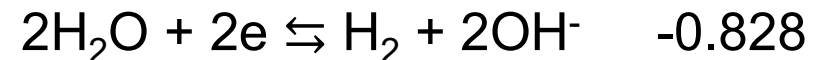
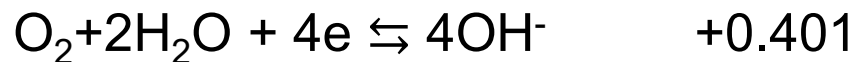
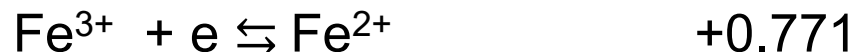
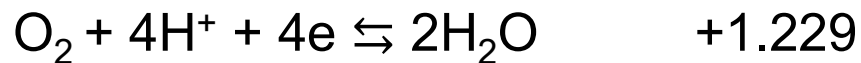
Standard electrode potentials

Aqueous Solutions at 25°C in V vs. SHE (standard hydrogen electrode), 1atm, $C^0=1M$



Standard electrode potentials

Aqueous Solutions at 25°C in V vs. SHE (standard hydrogen electrode), 1atm, **C⁰=1M**

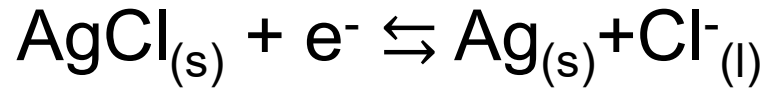


For the previous case:

$$V = (-0.762\text{V}) - (+0.222\text{V}) = -0.984\text{V}$$

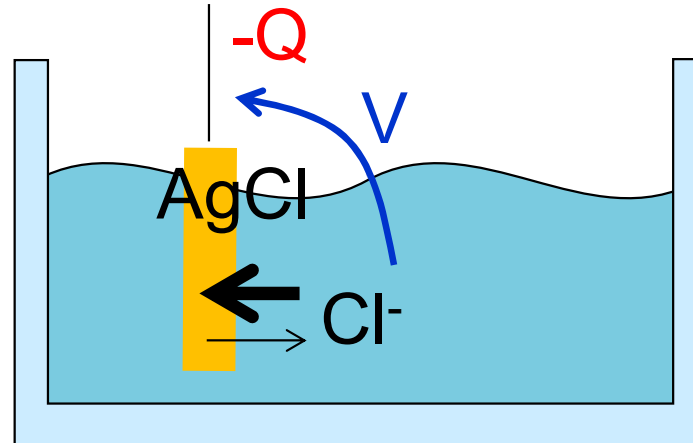
Eq. potential: role of the concentration

Ex.: AgCl electrode immersed in a solution with Cl^- (C_{Cl^-}):



$$C_{\text{Cl}^-} > C_{\text{Cl}^-,0}$$

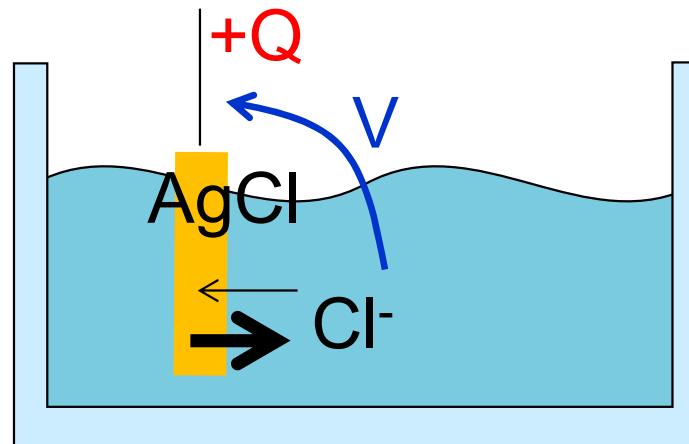
(AgCl production)



equilibrium
condition:
 $V < V_0$

$$C_{\text{Cl}^-} < C_{\text{Cl}^-,0}$$

(AgCl dissolves)

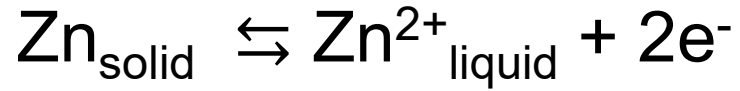


equilibrium
condition:
 $V > V_0$

Assuming a Boltzmann dist.: $V = V_0 \left(-\frac{kT}{q} \log \left(\frac{C_{\text{Cl}^-}}{C_{\text{Cl}^-,0}} \right) \right)$

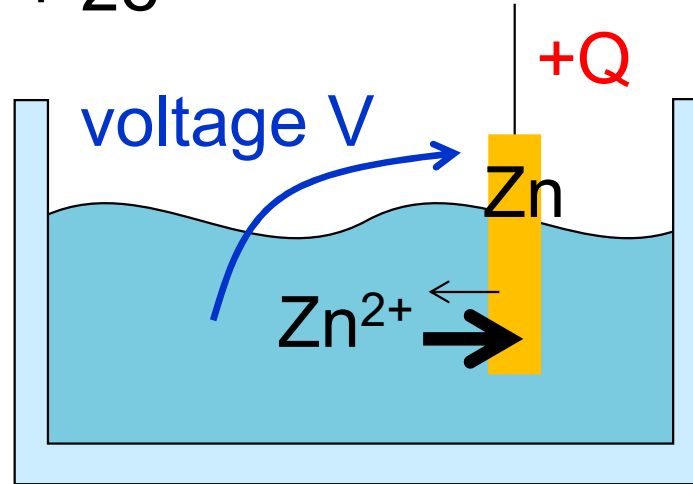
Eq. potential: role of the concentration

Ex.: Zn electrode immersed in a solution with Zn^{2+} ($C_{\text{Zn}^{2+}}$):



$$C_{\text{Zn}^{2+}} > C_{\text{Zn}^{2+},0}$$

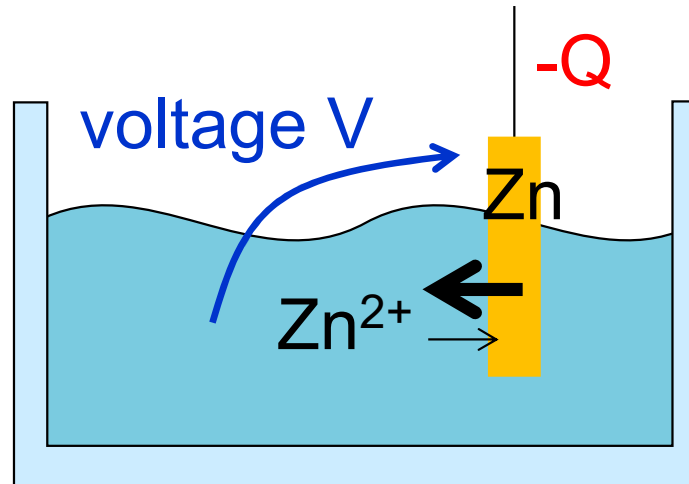
(Zn deposition)



equilibrium
condition:
 $V > V_0$

$$C_{\text{Zn}^{2+}} < C_{\text{Zn}^{2+},0}$$

(Zn dissolves)

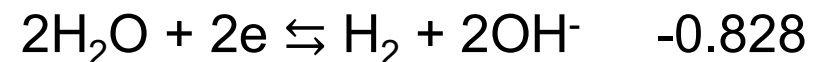
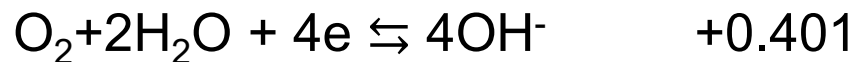
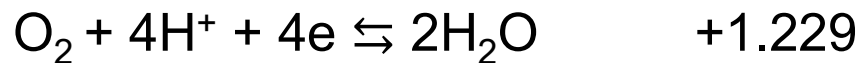


equilibrium
condition:
 $V < V_0$

Assuming a Boltzmann dist.: $V = V_0 + \frac{kT}{2q} \log \left(\frac{C_{\text{Zn}^{2+}}}{C_{\text{Zn}^{2+},0}} \right)$

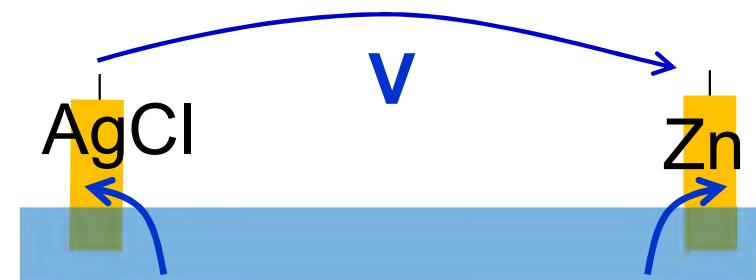
Nernst equation

Aqueous Solutions at 25°C in V vs. SHE, 1atm, $C^0=1M$



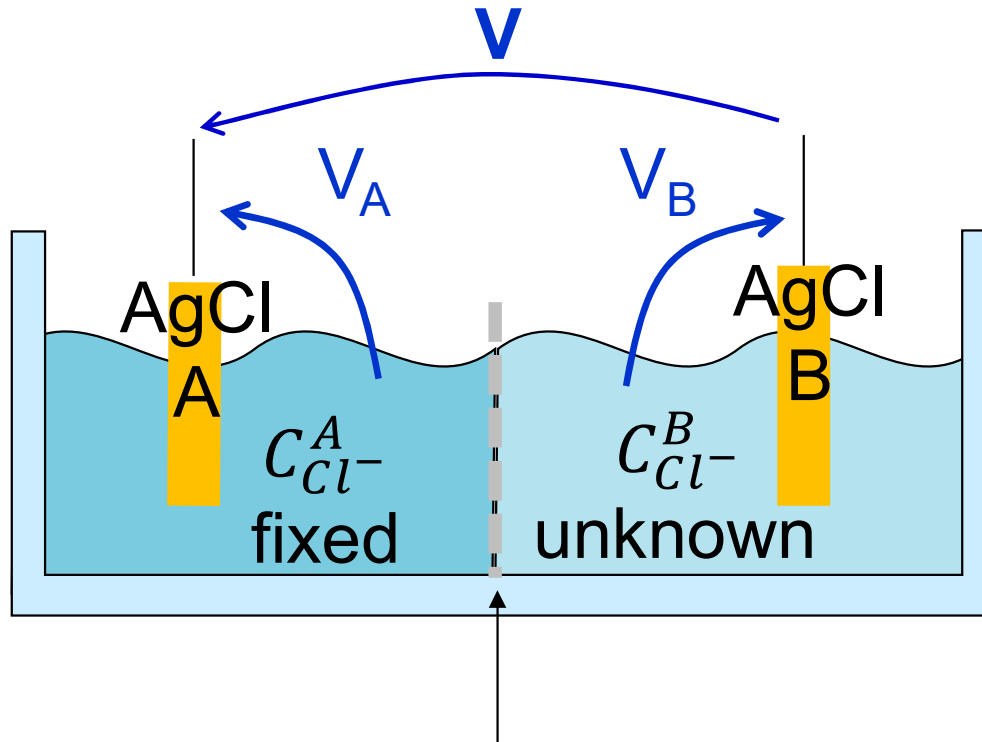
For the previous case:

$$V = -0.762V + \frac{kT}{2q} \ln \left(\frac{C_{Zn^{2+}}}{C^0} \right) - \left[+0.222V - \frac{kT}{q} \ln \left(\frac{C_{Cl^-}}{C^0} \right) \right]$$



Potentiometric sensor

Measure of concentration:



ion-selective membrane

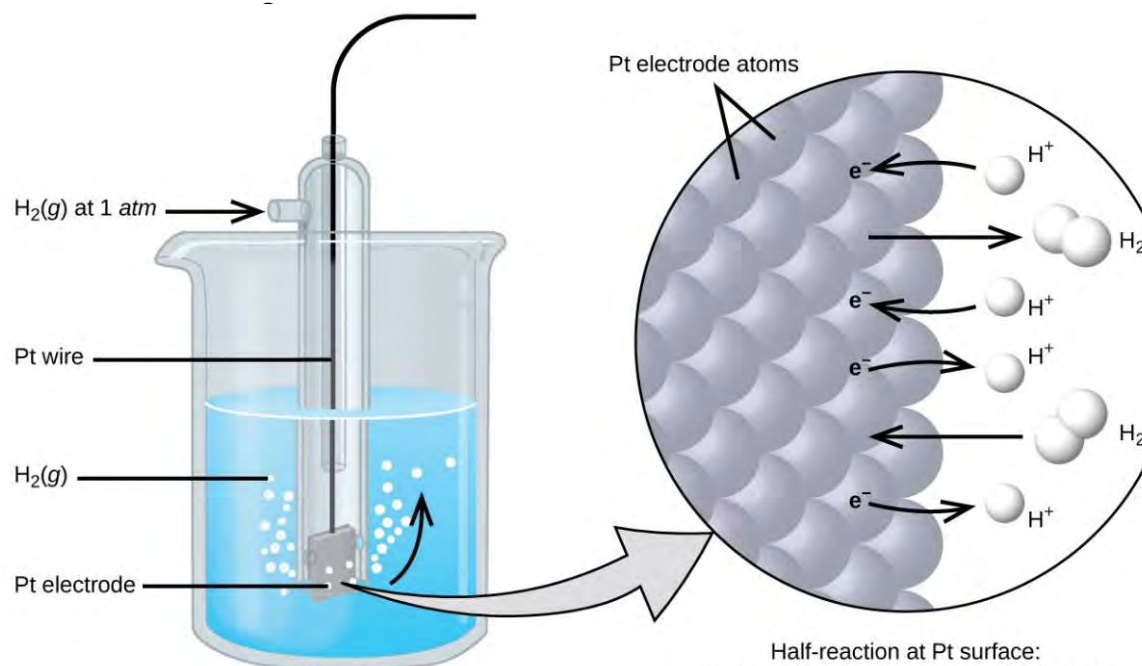
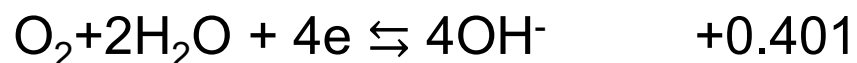
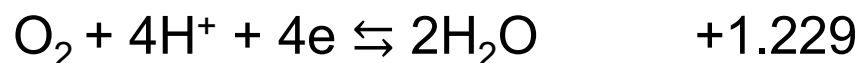
equilibrium condition ($I=0$)

$$V_A = V_0 - \frac{kT}{q} \ln \left(\frac{C_{Cl^-}^A}{C^0} \right)$$
$$V_B = V_0 - \frac{kT}{q} \ln \left(\frac{C_{Cl^-}^B}{C^0} \right)$$
$$V = V_A - V_B = \frac{kT}{q} \ln \left(\frac{C_{Cl^-}^B}{C_{Cl^-}^A} \right)$$

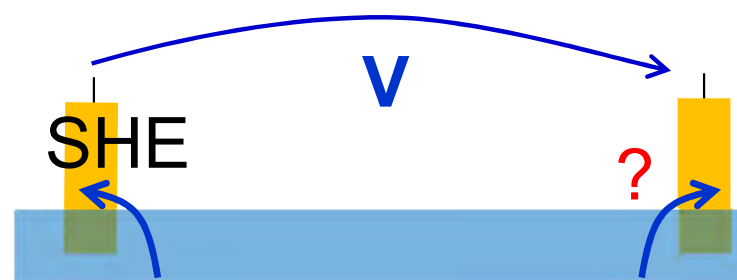
$$V \propto \ln(C_{Cl^-}^B)$$

Standard electrode potentials

Aqueous Solutions at 25°C in V vs. **SHE** (standard hydrogen electrode), 1atm, **C⁰=1M**



Half-reaction at Pt surface:
 $2\text{H}^+(\text{aq}, 1\text{ M}) + 2\text{e}^- \rightarrow \text{H}_2(\text{g}, 1\text{ atm})$



Reference electrodes

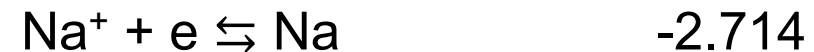
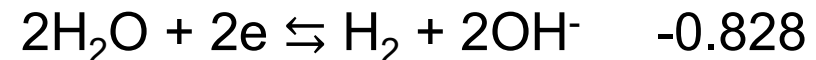
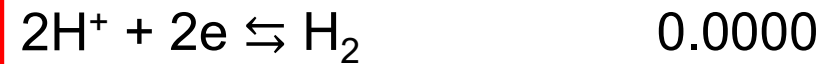
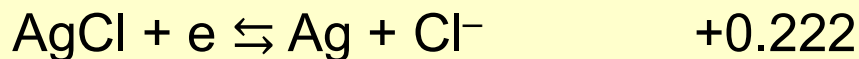
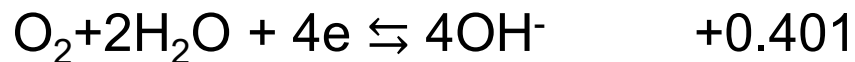
Purpose: provide a **stable potential** against which other potentials can be reliably measured

Criteria:

- stable in potential (time, temperature)
- chemical reactions at the surface are reversible
- potential shouldn't be altered by passage of small current = not polarizable
- reproducible
- easy fabrication and handling
- convenient for use

Reference electrodes

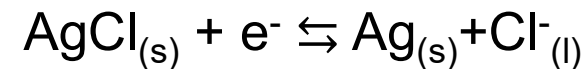
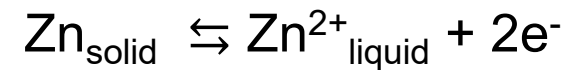
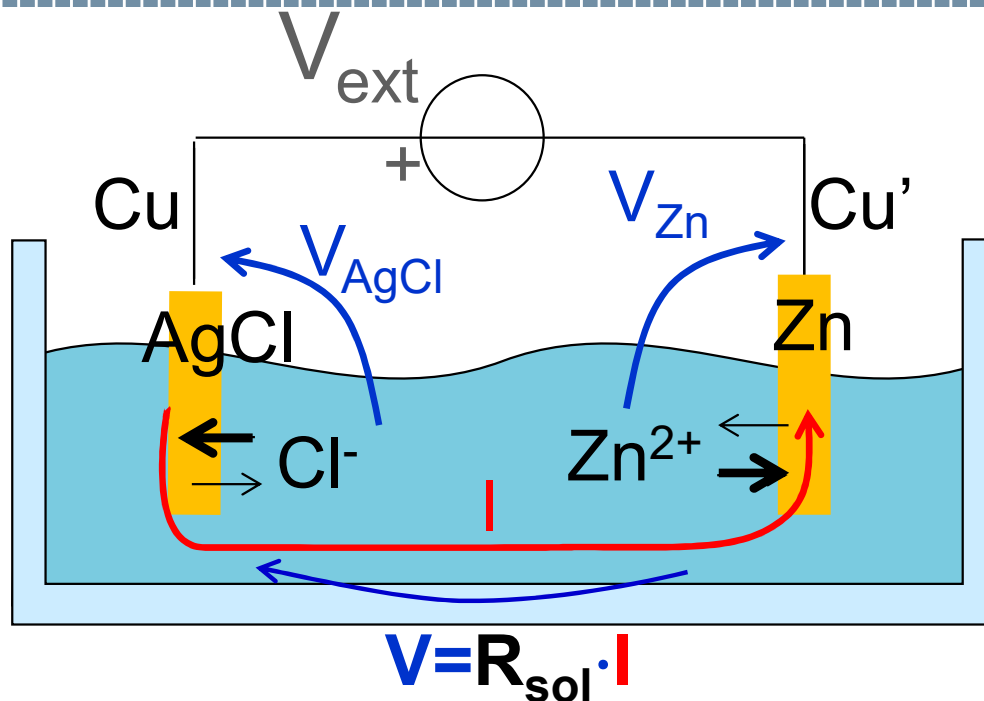
Aqueous Solutions at 25°C in V vs. SHE, 1atm, C⁰=1M



Saturated Calomel Electrode (SCE):
+0.244

Ag wire coated with AgCl(s), immersed in NaCl or KCl solution. It is stable in a solution with a large quantity of Cl⁻ such as the [biological fluid \(e.g. PBS\)](#).

Out-of-equilibrium condition



$$V_{ext} = V_{AgCl} + R_{sol} \cdot I - V_{Zn}$$

By forcing $V_{ext} >$ equilibrium voltage

→ more Cl^- are attracted on the left ($V_{AgCl} \uparrow$)

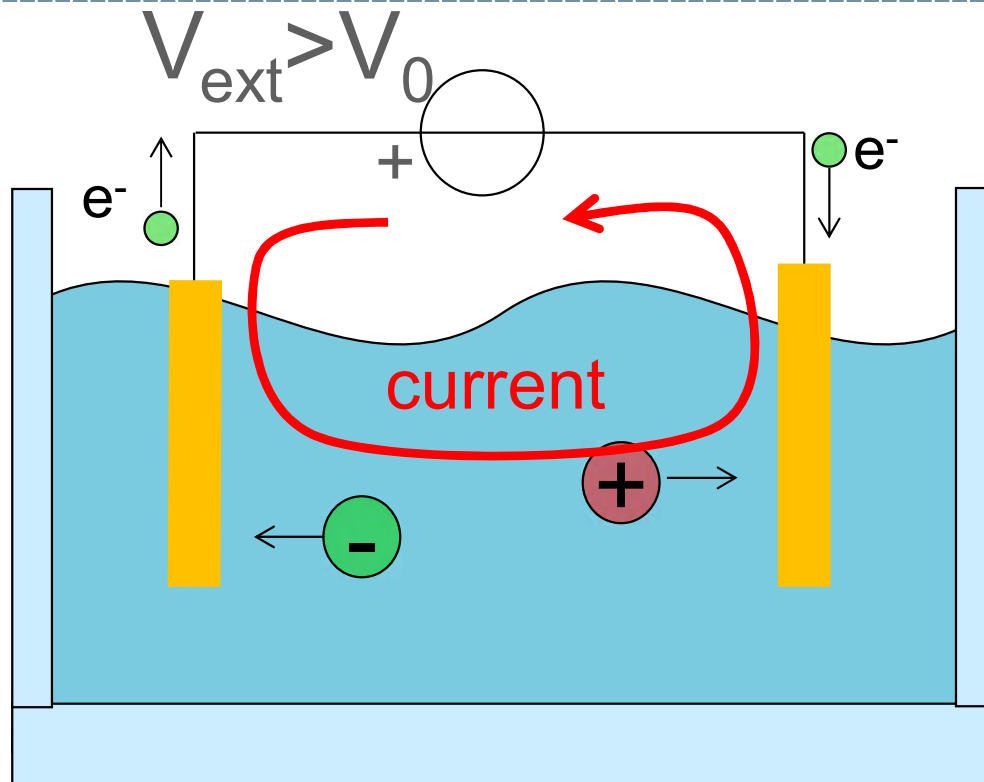
more Zn^{2+} are attracted on the right ($V_{Zn} \downarrow$)

→ chemical equilibrium is broken

→ current

Note: no direct control of the voltage drop at metal-liquid interface

Electrical current in ionic conductors



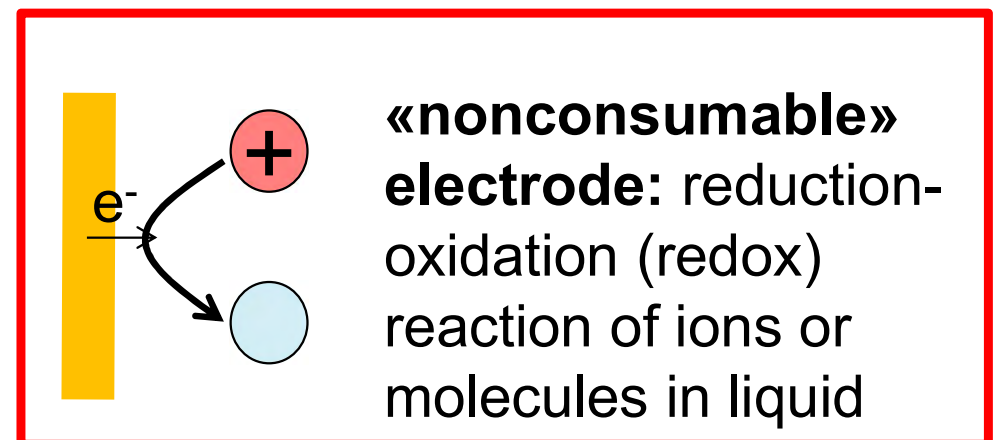
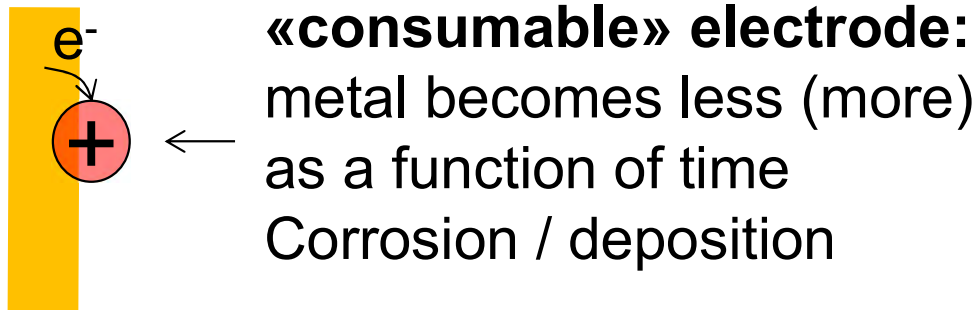
Ions move in the liquid

Electrons move in the electrodes

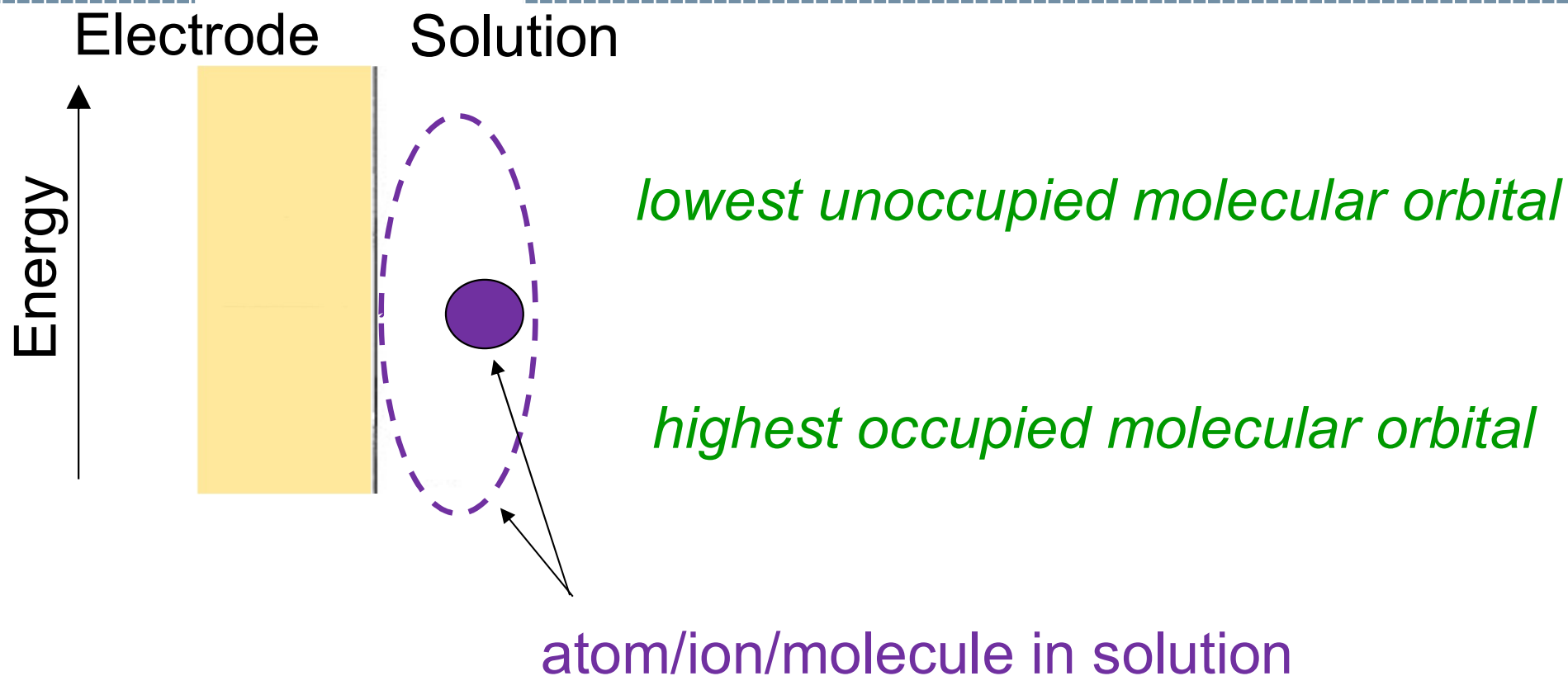


Chemical reactions
with **electron transfer**
at the metal/liquid interfaces

Two main cases:

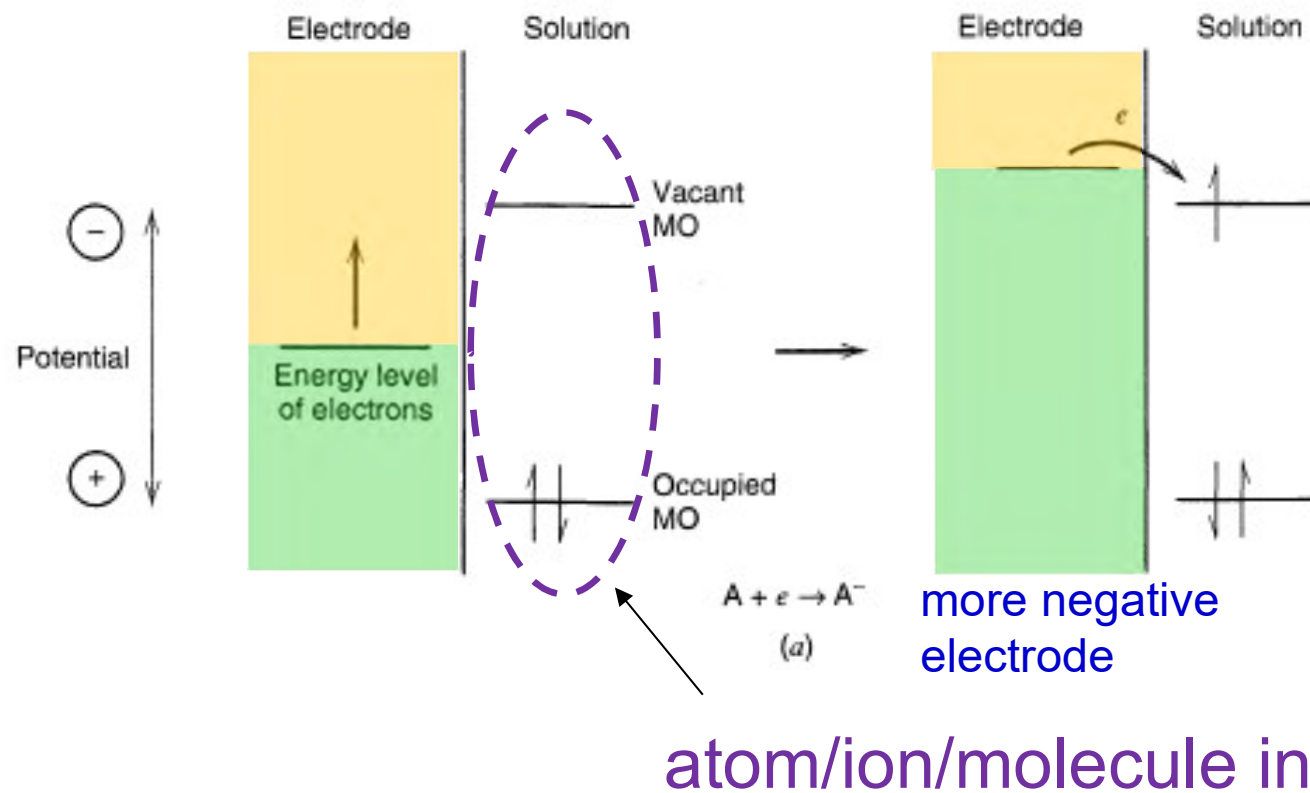


Electron Transfer



Bard, Electrochemical methods.
Fundamentals and applications

Electron Transfer

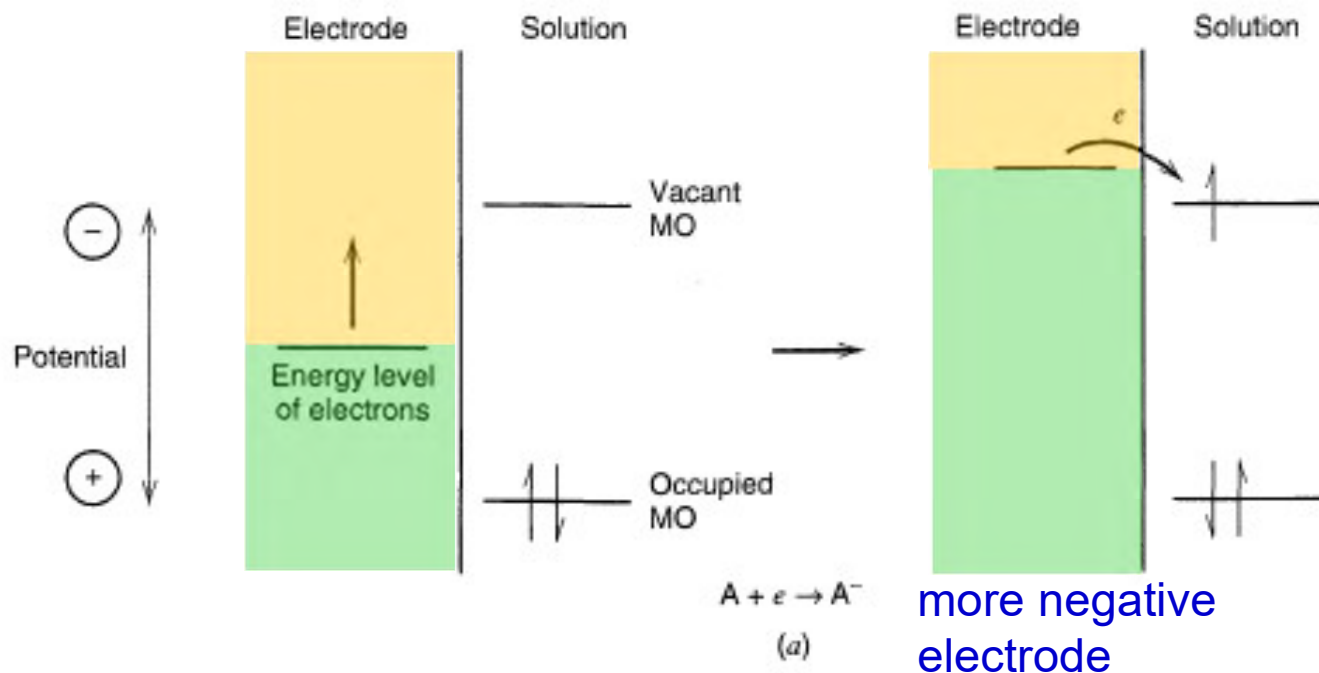


Reduction:
atom/ion/molecule
gains an electron

reaction controlled by
the potential drop
across the interface

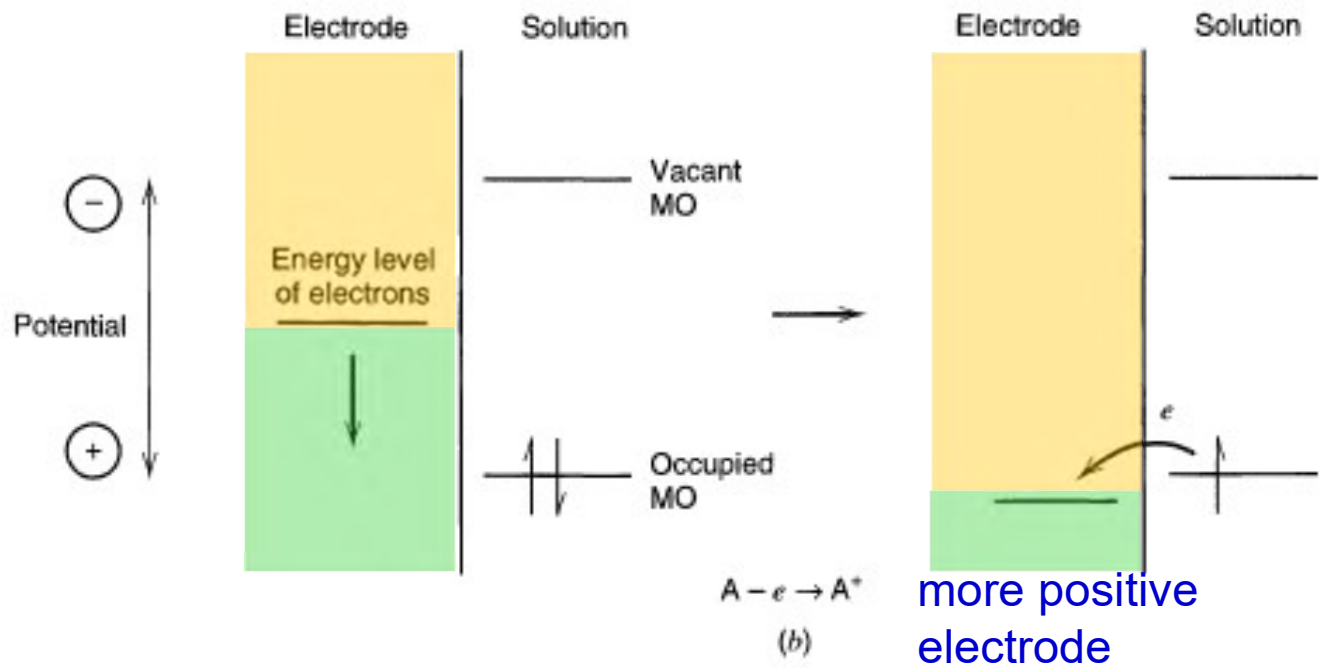
Bard, Electrochemical methods.
Fundamentals and applications

Electron Transfer



Reduction:
atom/ion/molecule
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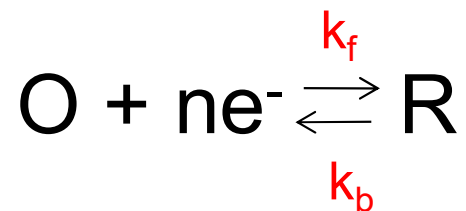


Oxidation:
atom/ion/molecule
loses an electron

Bard, Electrochemical methods.
Fundamentals and applications

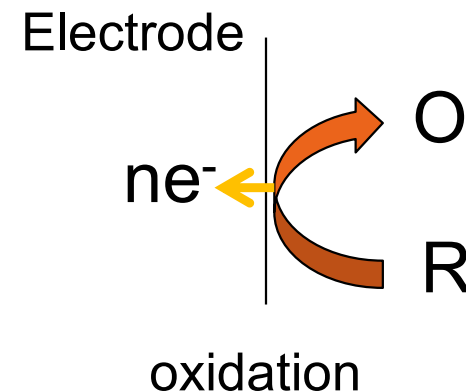
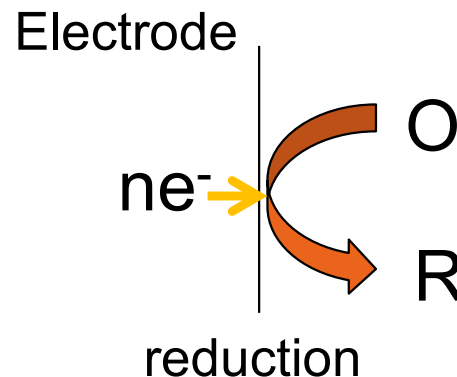
The Kinetics of Electron Transfer

Consider:



Assume:

- O and R are stable, soluble
- no competing chemical reactions occur



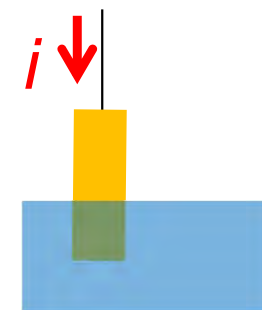
number of reductions per second $\propto \underbrace{N_{Av} C_O A}_{\substack{\text{number of O} \\ \text{near the electrode} \\ [C_O] = [\text{mol}/\text{cm}^3]}} \rightarrow = \underbrace{k_f}_{\substack{\text{rate constant} \\ (\text{cm}/\text{s})}} N_{Av} C_O A$

$A = \text{area of the electrode } [\text{cm}^2]$

number of oxidations per second = $k_b N_{Av} C_R A$

$$i = i_b - i_f = nq [k_b N_{Av} A C_R(0) - k_f N_{Av} A C_O(0)]$$

Sign convention:

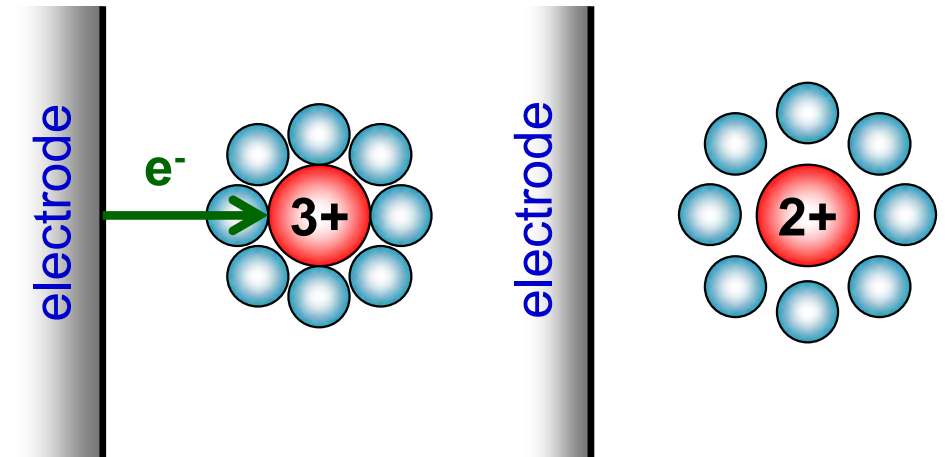
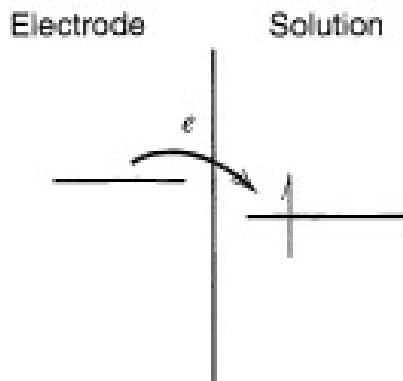


Marcus / Gerischer microscopic model

(1992 Nobel prize in chemistry)

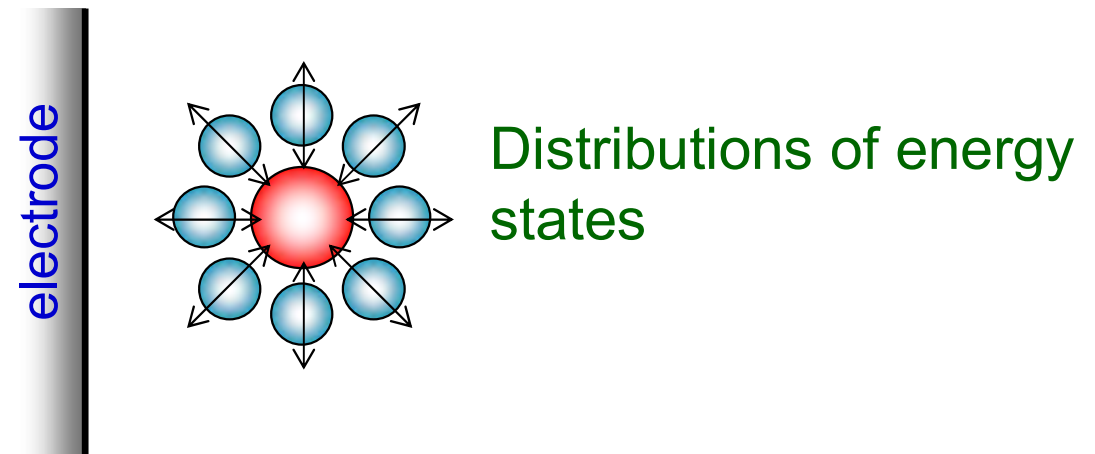
- **Tunneling** between states in the electrode and those of the ion/molecule

- reorganization energy (λ)



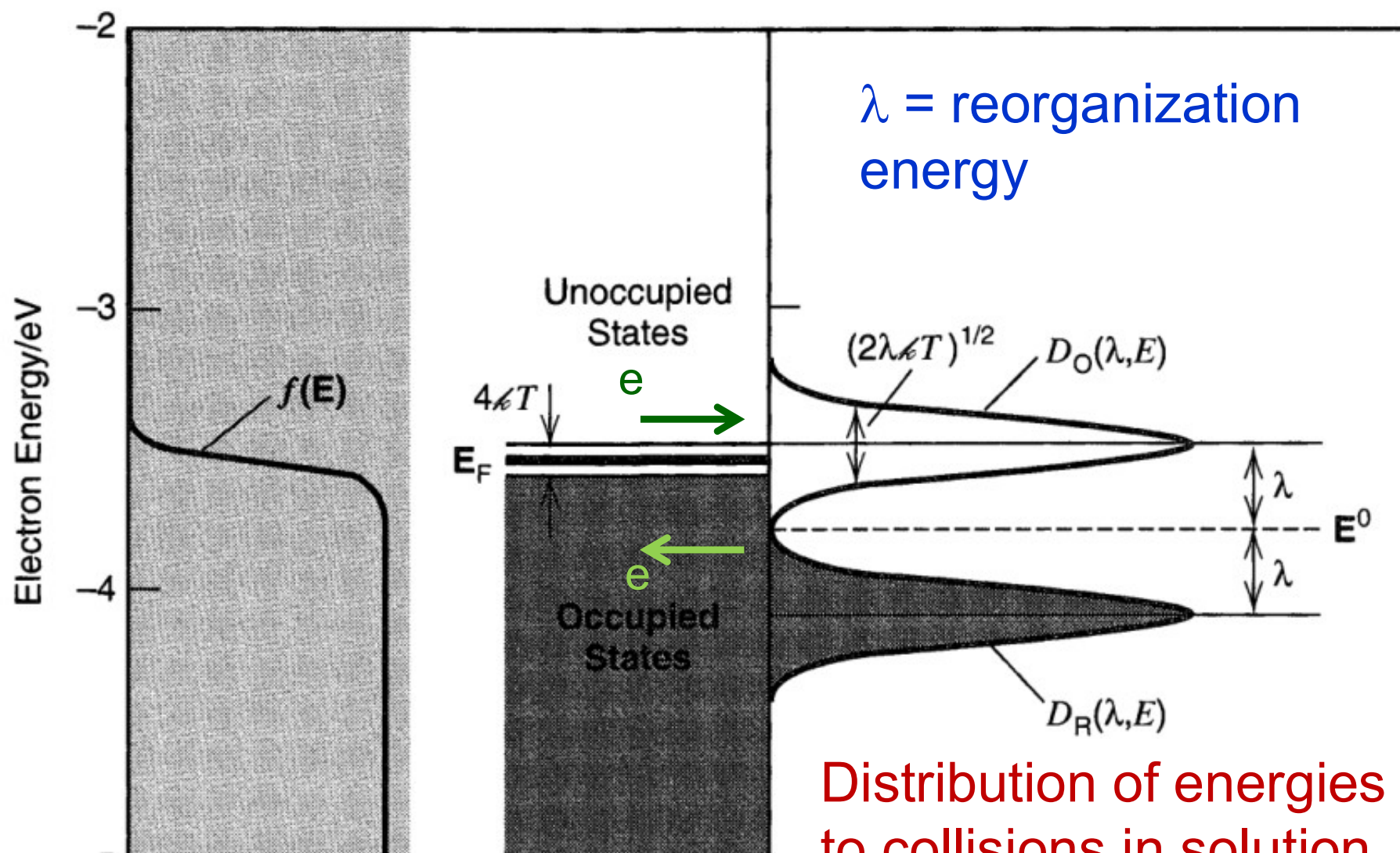
Two different energy levels

- fluctuations of the solvent molec.



Distributions of energy states

Electron Transfer: Gerischer view

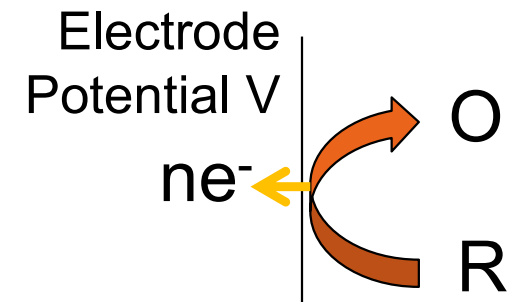
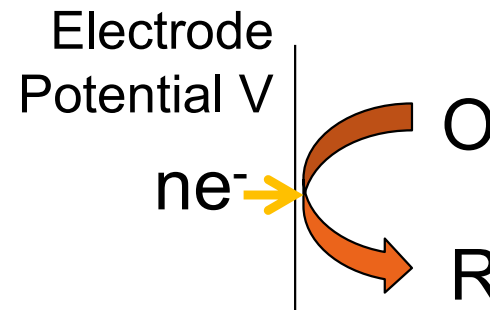
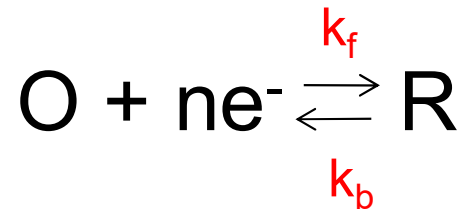


$$k_f \propto \int_{-\infty}^{+\infty} \frac{e^{-\left(x - \frac{\lambda + (V - V^0)}{kT}\right)^2 \frac{kT}{4\lambda}}}{1 + e^x} dx$$

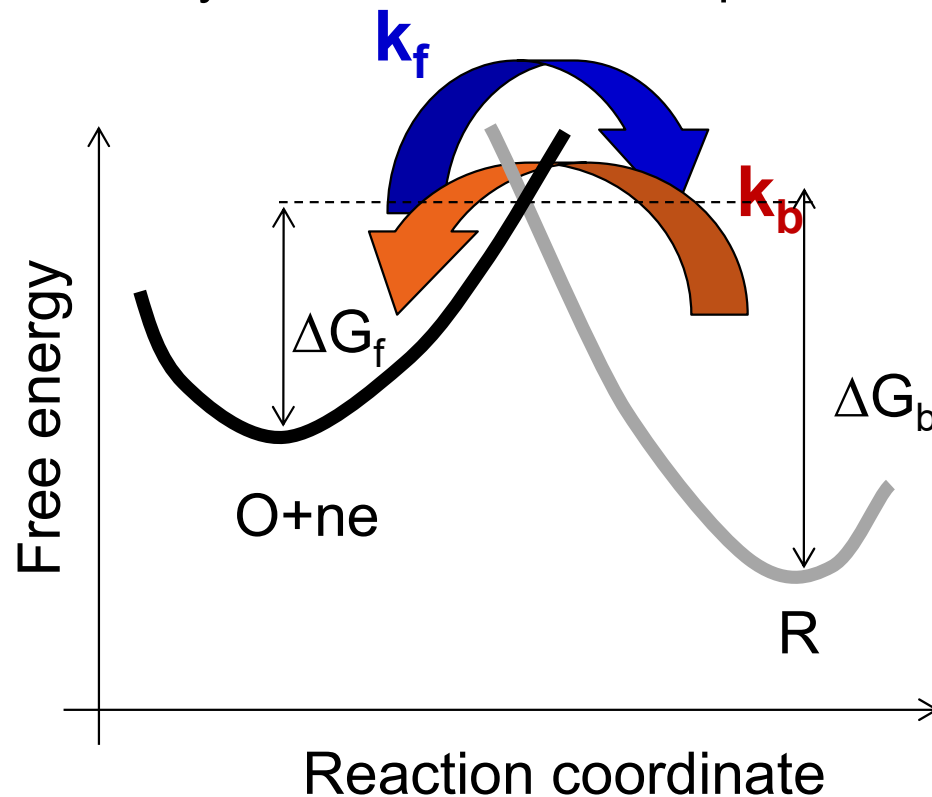
Reactant States

The Thermodynamics of Electron Transfer

Consider:



Arrhenius theory: an energy barrier has to be surmounted by the reactants before they can be converted to product

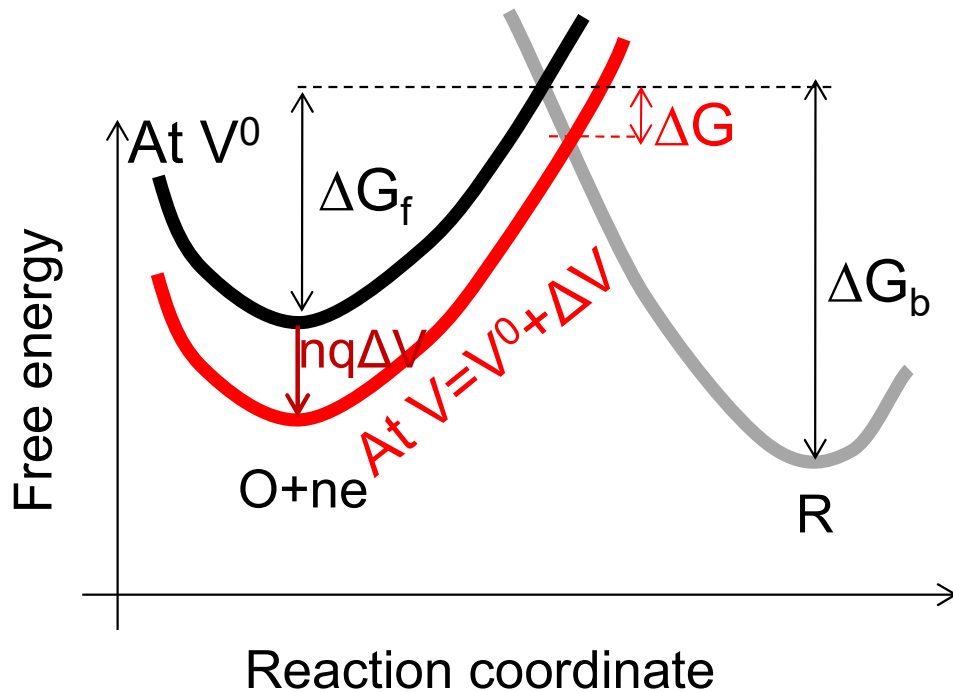


Arrhenius equation:

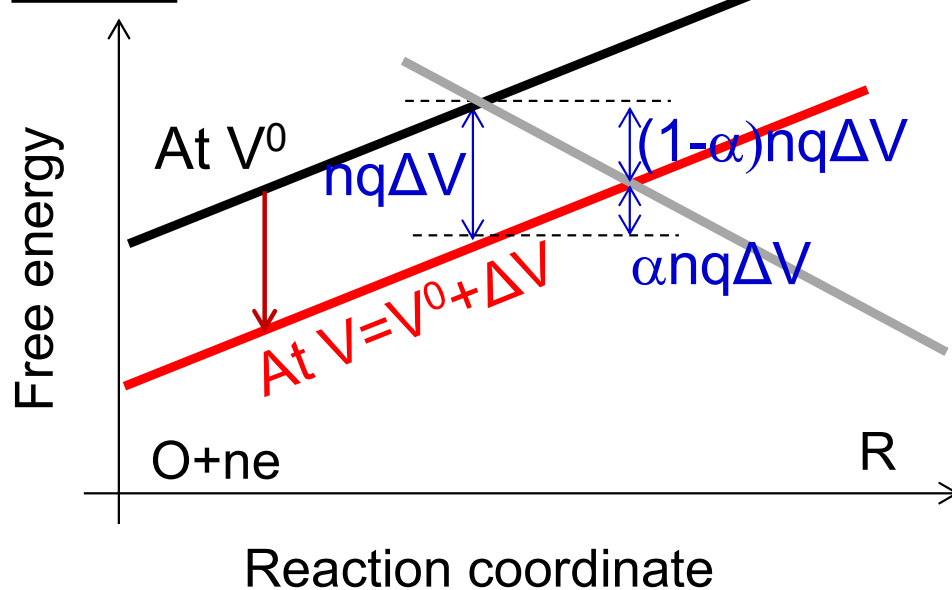
$$k_f = A_f e^{-\frac{\Delta G_f}{kT}}$$

$$k_b = A_b e^{-\frac{\Delta G_b}{kT}}$$

Effect of the voltage on the energy barrier



Zoom:



Linearization of curves:

ΔG is prop. to ΔV



$$\Delta G_f = \Delta G_f^0 + nq\Delta V - (1 - \alpha)nq\Delta V$$

$$\Delta G_b = \Delta G_b^0 - (1 - \alpha)nq\Delta V$$

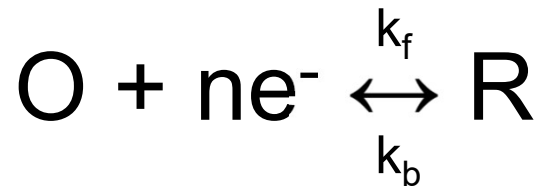
$$k_f = k_0 e^{-\frac{\alpha nq(V - V^{0'})}{kT}}$$

$$k_b = k_0 e^{\frac{(1-\alpha)nq(V - V^{0'})}{kT}}$$

α = transfer coefficient, about 0.5
 $V^{0'}$ = formal potential of the reaction: $k_f = k_b$

k_0 = standard rate constant

Electronic current



$$i = i_b - i_f = nqN_{Av} A [k_b C_R(0) - k_f C_O(0)]$$

A = surface area
C(0) = concentration
at the electrode

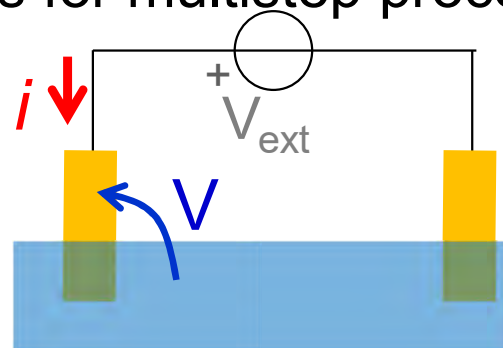
$$i = nqN_{Av} A k_0 \left[C_R(0) e^{(1-\alpha)nq(V-V^0')/kT} - C_O(0) e^{-\alpha nq(V-V^0')/kT} \right]$$

Butler-Volmer formulation of electrode kinetics

Typical values:

- $\alpha \approx 0.5$
- k_0 : 1-10 cm/s for simple electron transfer
10⁻⁶ cm/s or less for multistep process with molecular rearrangement

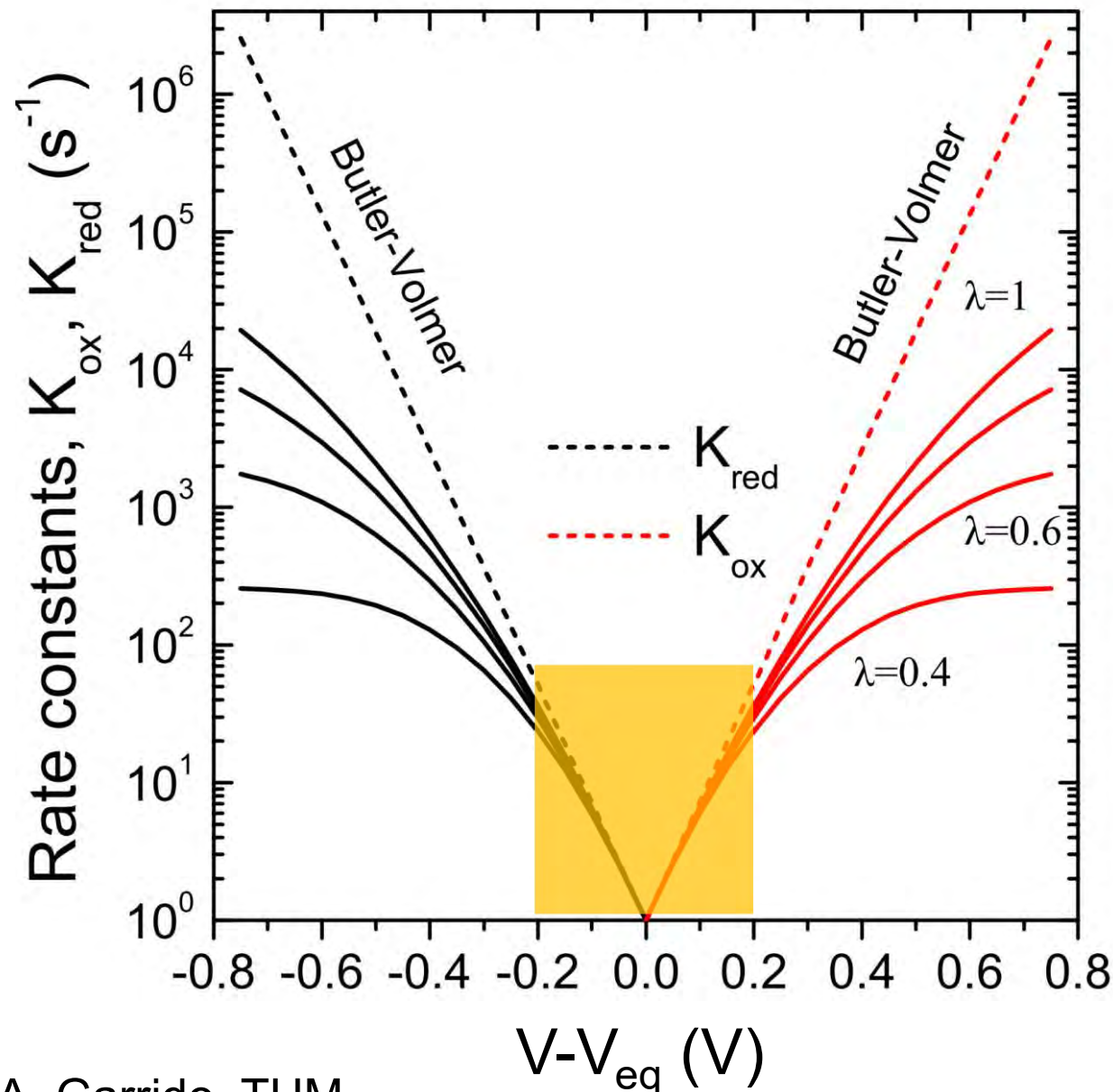
Sign convention:



$$V = V_{\text{ext}} - R_{\text{sol}} \cdot i - V_{\text{2nd electrode}}$$

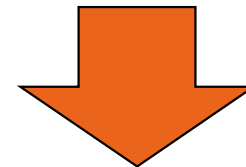
(see Carminati's lesson on how to better control V using V_{ext})

Marcus / Gerischer model vs Butler-Volmer



typical λ : 0.5eV – 1eV

measurable kinetics
usually corresponds to
a ΔV_{max} of 50-200mV



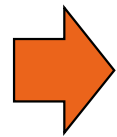
Butler-Volmer is
accurate enough

...kinetic is not the only
parameter controlling the
current ! (next lesson)

Equilibrium condition

$$i = nqN_{Av}Ak_0 \left[C_R(0)e^{(1-\alpha)nq(V-V^{0'})/kT} - C_O(0)e^{-\alpha nq(V-V^{0'})/kT} \right]$$

At equilibrium, no net current flows: $i = i_b - i_f = 0$



$$V_{eq} = V^{0'} + \frac{kT}{nq} \ln \left(\frac{C_O}{C_R} \right)$$

Nernst equation

Dynamic equilibrium : $O + ne^- \rightarrow R$, $R - ne^- \rightarrow O$

both processes will occur **at equal rates**:

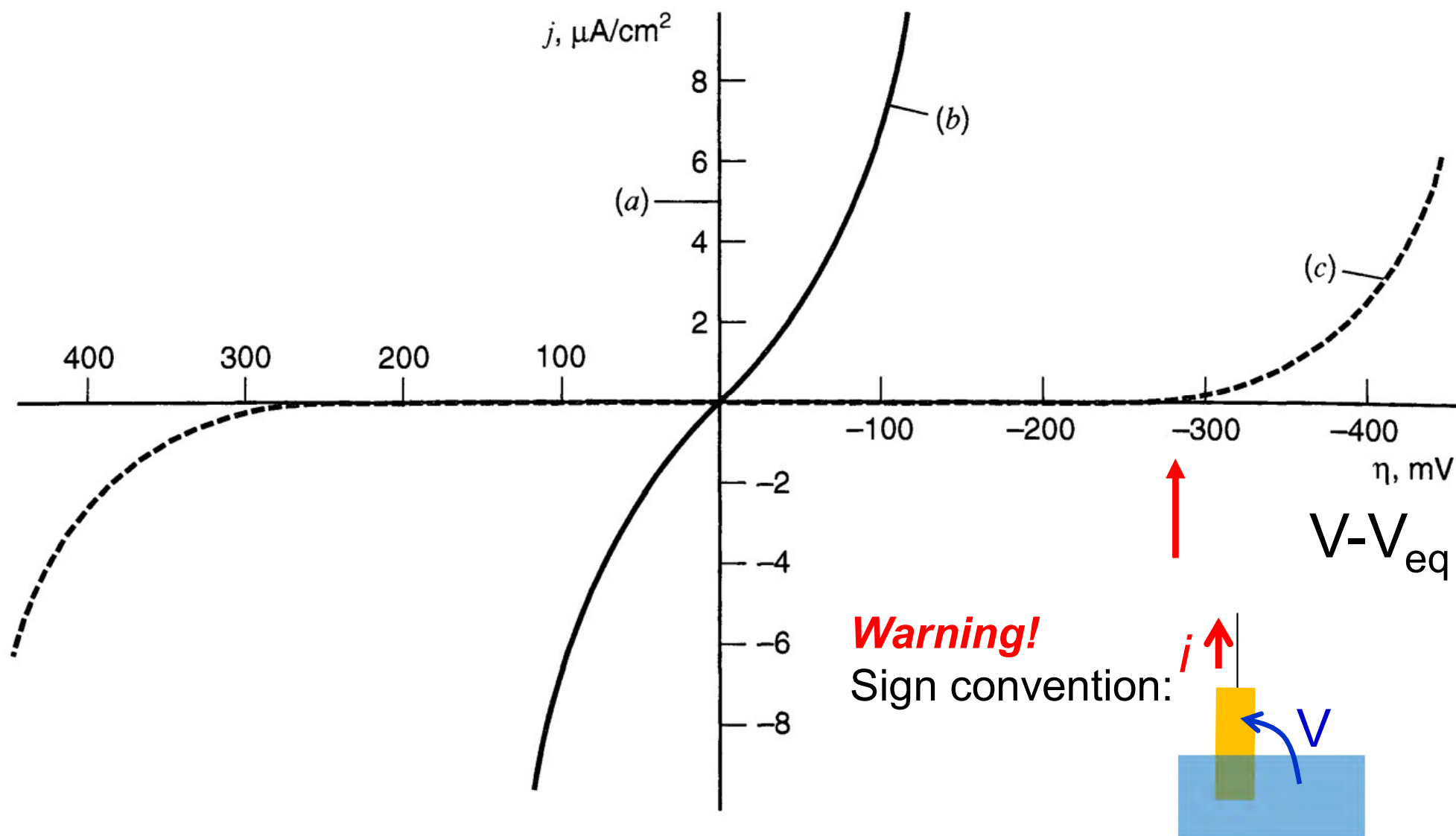
$$i_f = i_b = i_0 = nqN_{Av}Ak_0 C_O e^{-\alpha nq(V_{eq}-V^{0'})/kT} = nqN_{Av}Ak_0 C_O^{1-\alpha} C_R^\alpha$$

$i_0 =$ exchange current

$$i = i_0 \left(e^{(1-\alpha)nq(V-V_{eq})/kT} - e^{-\alpha nq(V-V_{eq})/kT} \right)$$

(it is the same equation!)

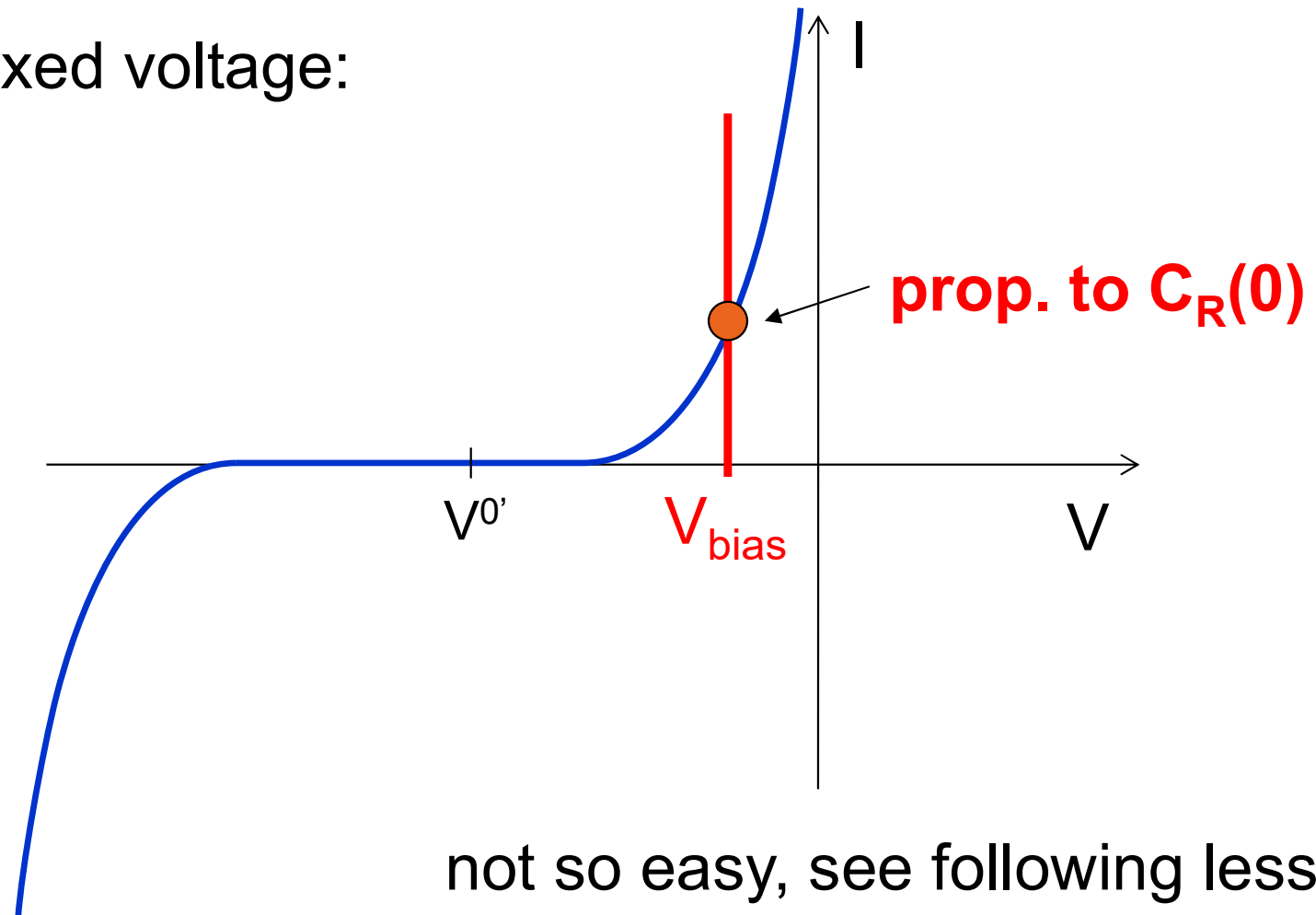
Kinetic controlled current



$\alpha=0.5$; (a) $i_0 = 10^{-3} \text{ A}/\text{cm}^2$; (b) $i_0 = 10^{-6} \text{ A}/\text{cm}^2$; (c) $i_0 = 10^{-9} \text{ A}/\text{cm}^2$

Amperometric sensor

Operating at fixed voltage:



not so easy, see following lessons!

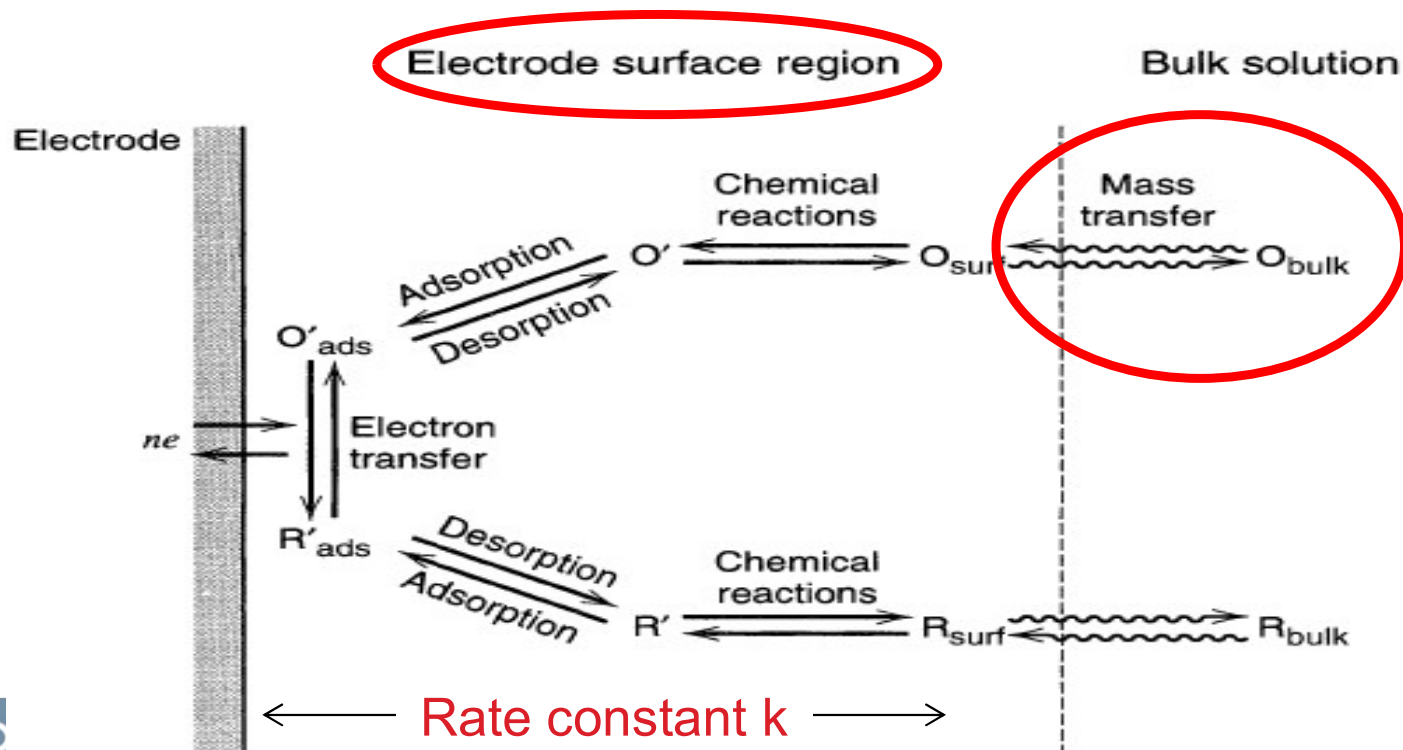
Butler-Volmer equation: concentrations at the surface

$$i = nqN_{Av}Ak_0 \left[C_R(0)e^{(1-\alpha)nq(V-V^{0'})/kT} - C_O(0)e^{-\alpha nq(V-V^{0'})/kT} \right]$$

An Interfacial Process

For: $\text{O} + n\text{e}^- \leftrightarrow \text{R}$ 5 separate events must occur:

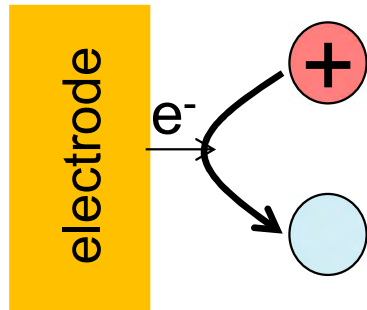
- O must be successfully transported from bulk solution (mass transport)
- O must adsorb transiently onto electrode surface (non-faradaic); Chemical reactions preceding or following the electron transfer (e.g., protonation or dimerization or catalytic decomposition) on the electrode surface.
- CT must occur between electrode and O (faradaic)
- R must desorb from electrode surface (non-faradaic)
- R must be transported away (mass transport)



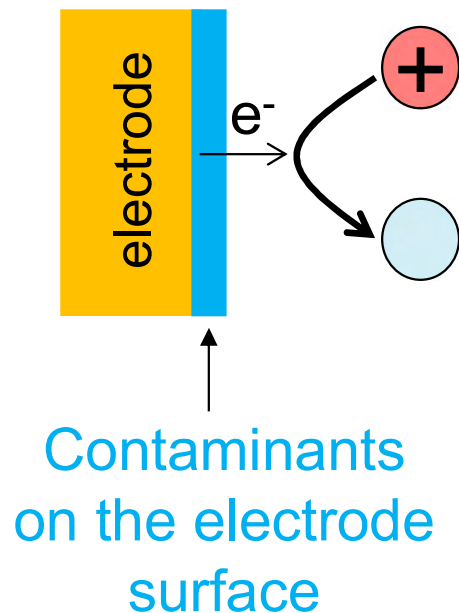
Next lesson

Bard, Electrochemical methods. Fundamentals and applications

Do not forget electrode pretreatments!



The electron transfer of a redox reaction is a tunneling process



The rate constant is exponentially related to the electrode – molecule distance



≈ nm thick contaminant can drastically reduce the electron transfer rate

Cleanliness is fundamental

Kinetics (and double layer) are controlled by the surface

→ electrodes must be carefully cleaned before each experiment:

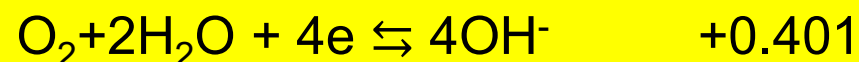
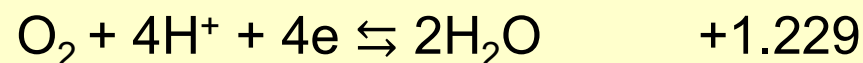
- Mechanical polishing (alumina), ultrasonic cleaning, plasma
- Chemical
 - Sonicate in acetone
 - Soak in HNO_3 , aqua regia
 - ...
- Electrochemical
 - Oxidation/reduction cycles in 0.5 M H_2SO_4 (Pt)
 - Oxidation/reduction cycles (-0.2V – +1.2V vs Ag/AgCl) in 50mM KOH (Au)
 - ...

Oxygen reduction can interfere with the measurement

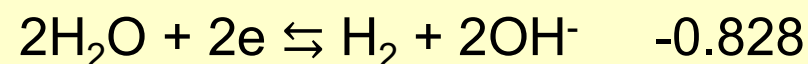
→ removal by purging with an inert gas

Limited electrochemical window

Aqueous Solutions at 25°C in V vs. SHE, 1atm, C⁰=1M



oxygen and pH can interfere!



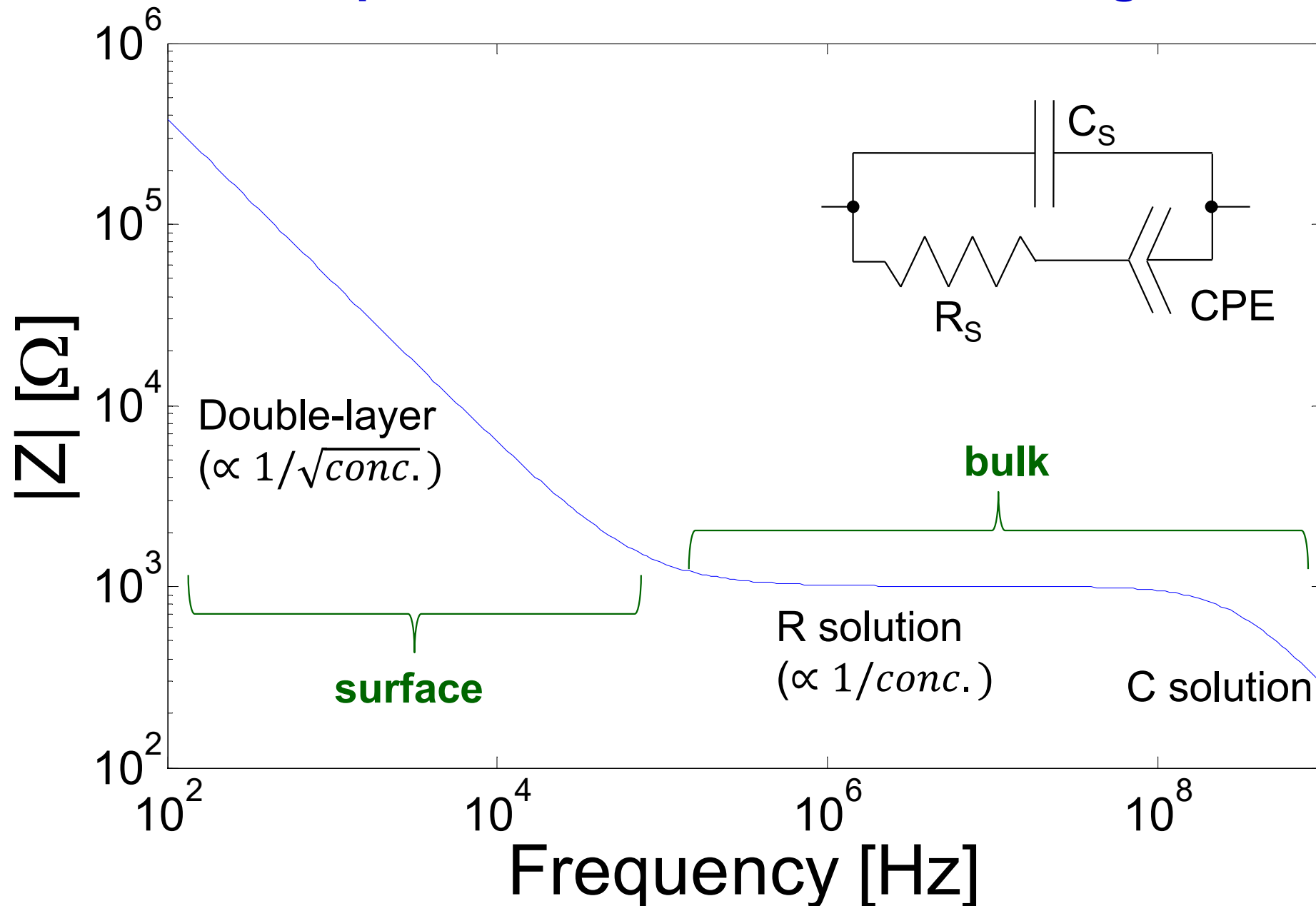
water electrolysis!



Experiment in water are typically limited at ΔV less than 2V
($\approx -1\text{V} < V < \approx 1\text{V}$ vs AgCl)

What about impedance spectra?

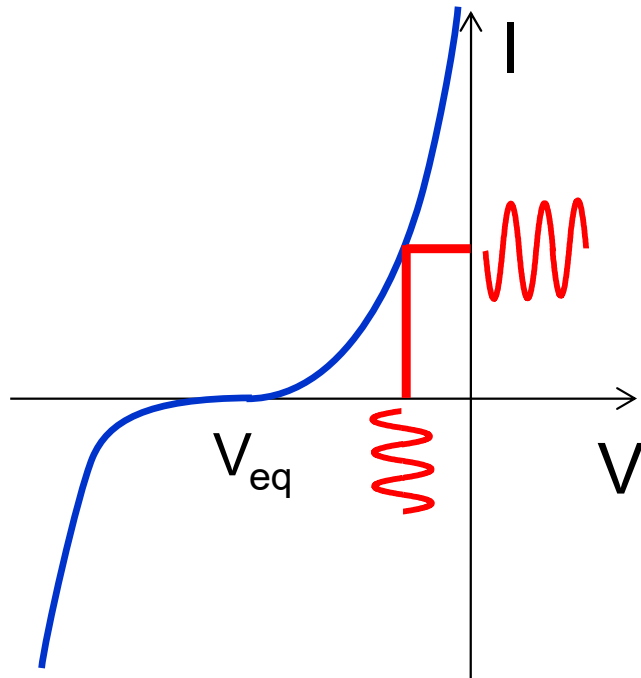
From the previous lesson **WITHOUT** charge transfer



Equivalent Circuit: Charge Transfer

The impedance concept requires a linear system
Electrode kinetics gives a non-linear behavior

Small signal
↓
linearization



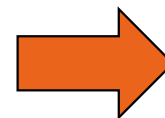
Charge transfer resistance:

$$R_{ct} = \left. \frac{\partial V}{\partial i} \right|_{\text{working point}}$$

$$i = i_0 \left(e^{(1-\alpha)nq(V-V_{eq})/kT} - e^{-\alpha nq(V-V_{eq})/kT} \right)$$

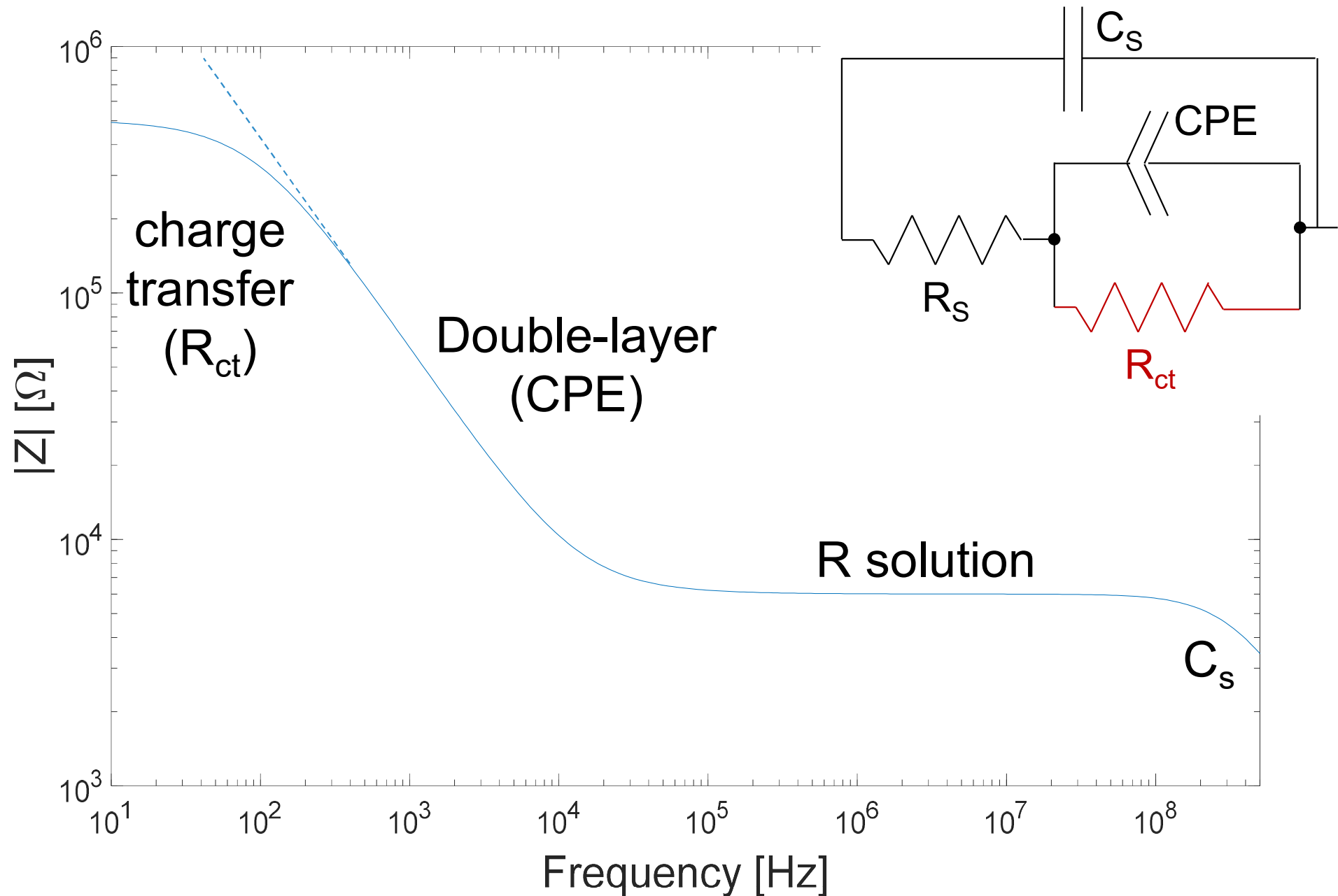
$$i_0 = nqN_{Av}Ak_0C_O^{1-\alpha}C_R^\alpha$$

A stationary condition is more easily obtained with $V \approx V_{eq}$



$$R_{ct} \approx \frac{kT}{nq} \frac{1}{i_0}$$

Impedance spectrum



Summary

- Equilibrium potential at the electrode-liquid interface
 - $I=0$ does not imply external voltage = 0V!
 - **Equilibrium potential** depends **on metals involved, ion species and ion concentrations** → **standard potentials, Nernst equation**
 - You never measure the single liquid-metal potential → at least two electrodes → reference electrode (AgCl)
- Electron transfer at the interface is possible:
 - Corrosion / deposition of the metal or **redox process at the metal-liquid interface**
 - **Exponential current-voltage characteristic** controlled by $V-V^0$ and by **concentrations** of species O and R at the surface
 - Empiric **Butler-Volmer** relation is accurate enough in many cases
 - Impedance: charge transfer resistance in parallel to C_{dl}